

ALGEBRA

Lines

Slope of the line through $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Slope-intercept equation of line with slope m and y -intercept b :

$$y = mx + b$$

Point-slope equation of line through $P_1 = (x_1, y_1)$ with slope m :

$$y - y_1 = m(x - x_1)$$

Point-point equation of line through $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$:

$$y - y_1 = m(x - x_1) \quad \text{where } m = \frac{y_2 - y_1}{x_2 - x_1}$$

Lines of slope m_1 and m_2 are parallel if and only if $m_1 = m_2$.

Lines of slope m_1 and m_2 are perpendicular if and only if $m_1 = -\frac{1}{m_2}$.

Circles

Equation of the circle with center (a, b) and radius r :

$$(x - a)^2 + (y - b)^2 = r^2$$

Distance and Midpoint Formulas

Distance between $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Midpoint of $\overline{P_1P_2}$: $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

Laws of Exponents

$$\begin{array}{lll} x^m x^n = x^{m+n} & \frac{x^m}{x^n} = x^{m-n} & (x^m)^n = x^{mn} \\ x^{-n} = \frac{1}{x^n} & (xy)^n = x^n y^n & \left(\frac{x}{y}\right)^n = \frac{x^n}{y^n} \\ x^{1/n} = \sqrt[n]{x} & \sqrt[n]{xy} = \sqrt[n]{x} \sqrt[n]{y} & \sqrt[n]{\frac{x}{y}} = \frac{\sqrt[n]{x}}{\sqrt[n]{y}} \\ x^{m/n} = \sqrt[n]{x^m} = (\sqrt[n]{x})^m & & \end{array}$$

Special Factorizations

$$\begin{array}{l} x^2 - y^2 = (x + y)(x - y) \\ x^3 + y^3 = (x + y)(x^2 - xy + y^2) \\ x^3 - y^3 = (x - y)(x^2 + xy + y^2) \end{array}$$

Binomial Theorem

$$\begin{array}{l} (x + y)^2 = x^2 + 2xy + y^2 \\ (x - y)^2 = x^2 - 2xy + y^2 \\ (x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3 \\ (x - y)^3 = x^3 - 3x^2y + 3xy^2 - y^3 \\ (x + y)^n = x^n + nx^{n-1}y + \frac{n(n-1)}{2}x^{n-2}y^2 \\ \quad + \dots + \binom{n}{k}x^{n-k}y^k + \dots + nxy^{n-1} + y^n \end{array}$$

$$\text{where } \binom{n}{k} = \frac{n(n-1)\dots(n-k+1)}{1 \cdot 2 \cdot 3 \dots k}$$

Quadratic Formula

$$\text{If } ax^2 + bx + c = 0, \text{ then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Inequalities and Absolute Value

If $a < b$ and $b < c$, then $a < c$.

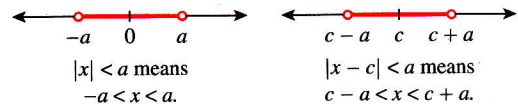
If $a < b$, then $a + c < b + c$.

If $a < b$ and $c > 0$, then $ca < cb$.

If $a < b$ and $c < 0$, then $ca > cb$.

$$|x| = x \quad \text{if } x \geq 0$$

$$|x| = -x \quad \text{if } x \leq 0$$

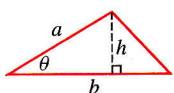


GEOMETRY

Formulas for area A , circumference C , and volume V

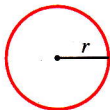
Triangle

$$\begin{array}{l} A = \frac{1}{2}bh \\ = \frac{1}{2}ab \sin \theta \end{array}$$



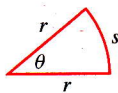
Circle

$$\begin{array}{l} A = \pi r^2 \\ C = 2\pi r \end{array}$$



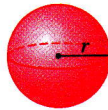
Sector of Circle

$$\begin{array}{l} A = \frac{1}{2}r^2\theta \\ s = r\theta \\ (\theta \text{ in radians}) \end{array}$$



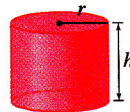
Sphere

$$\begin{array}{l} V = \frac{4}{3}\pi r^3 \\ A = 4\pi r^2 \end{array}$$



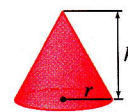
Cylinder

$$V = \pi r^2 h$$



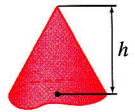
Cone

$$\begin{array}{l} V = \frac{1}{3}\pi r^2 h \\ A = \pi r \sqrt{r^2 + h^2} \end{array}$$



Cone with arbitrary base

$$\begin{array}{l} V = \frac{1}{3}Ah \\ \text{where } A \text{ is the area of the base} \end{array}$$



Pythagorean Theorem: For a right triangle with hypotenuse of length c and legs of lengths a and b , $c^2 = a^2 + b^2$.

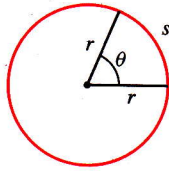
TRIGONOMETRY

Angle Measurement

$$\pi \text{ radians} = 180^\circ$$

$$1^\circ = \frac{\pi}{180} \text{ rad} \quad 1 \text{ rad} = \frac{180^\circ}{\pi}$$

$$s = r\theta \quad (\theta \text{ in radians})$$



Right Triangle Definitions

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

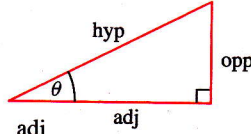
$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\text{opp}}{\text{adj}}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta} = \frac{\text{adj}}{\text{opp}}$$

$$\sec \theta = \frac{1}{\cos \theta} = \frac{\text{hyp}}{\text{adj}}$$

$$\csc \theta = \frac{1}{\sin \theta} = \frac{\text{hyp}}{\text{opp}}$$



Trigonometric Functions

$$\sin \theta = \frac{y}{r}$$

$$\csc \theta = \frac{r}{y}$$

$$\cos \theta = \frac{x}{r}$$

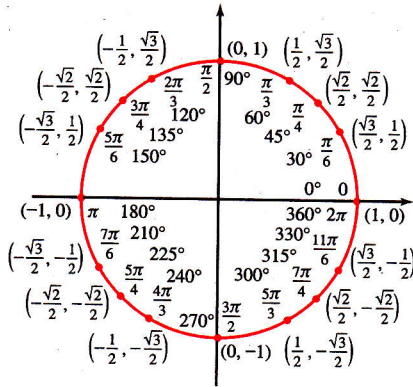
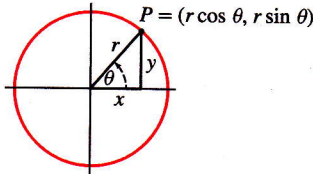
$$\sec \theta = \frac{r}{x}$$

$$\tan \theta = \frac{y}{x}$$

$$\cot \theta = \frac{x}{y}$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta} = 0$$



Fundamental Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin(-\theta) = -\sin \theta$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$\cos(-\theta) = \cos \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\tan(-\theta) = -\tan \theta$$

$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$$

$$\sin(\theta + 2\pi) = \sin \theta$$

$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$

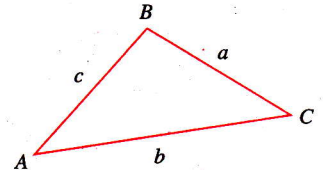
$$\cos(\theta + 2\pi) = \cos \theta$$

$$\tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta$$

$$\tan(\theta + \pi) = \tan \theta$$

The Law of Sines

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$



The Law of Cosines

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Addition and Subtraction Formulas

$$\sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\sin(x - y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

$$\cos(x - y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

Double-Angle Formulas

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

Graphs of Trigonometric Functions

